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## Liquid Crystals

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# Comparison of short range interactions in nematic liquid crystals $A^{\mathbf{2}} \mathbf{H}$-NMR study of $5 \mathrm{CB}-d_{19}$ as a solute 

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#### Abstract

Previous studies using dideuterium as a solute have demonstrated the importance for orientation of the interaction between the solute molecular quadrupole moment and the average electric field gradient present in liquid crystals. With the aim of learning about additional orientational mechanisms, we have studied the temperature dependence of the ${ }^{2} \mathrm{H}$-NMR spectra of the liquid crystal $5 \mathrm{CB}-d_{19}$ as the solute in three liquid crystal mixtures: $55 \mathrm{wt} \%$ 1132/EBBA, $56.5 \mathrm{wt} \%$ 1132/EBBA and $70 \mathrm{wt} \%$ 5CB/EBBA. In these mixtures, the contribution from the environment to the average electric field gradient at the ${ }^{2} \mathrm{H}$ nucleus of dideuterium is zero. The spectra of $5 \mathrm{CB}-d_{19}$ in the mixtures $55 \mathrm{wt} \% 1132 / \mathrm{EBBA}$ and $56.5 \mathrm{wt} \%$ 1132/EBBA are equivalent, but are different from those in $70 \mathrm{wt} \%$ 5CB/EBBA. The spectra of 5 CB in $55 \mathrm{wt} \% 1132 / \mathrm{EBBA}$ and $70 \mathrm{wt} \% 5 \mathrm{CB} / \mathrm{EBBA}$ are analysed using two different models for the short range potential, and parameters of the models are used to compare the potentials in the different mixtures. For a given spectral splitting of the chain $\mathrm{C}_{1}$ deuteron, the reduced short range potential is the same in all three mixtures studied. The spectral differences observed are a consequence of different nematic-isotropic phase transition temperatures combined with the effect of trans/gauche-isomerization in the hydrocarbon chain.


## 1. Introduction

A detailed understanding of anisotropic intermolecular interactions leading to orientational ordering in liquid crystal systems is not available. The situation is complicated by the size and flexibility of the liquid crystal molecules. In many cases, the intermolecular interactions are described by a mean field theory [1-3] in which the interaction potential is expressed in terms of model parameters.

The anisotropic interactions lead to an orientational ordering of the liquid crystal molecules. This orientational ordering can be described in terms of order parameters. Second rank order parameters can be measured by various techniques, including NMR (nuclear magnetic resonance) spectroscopy. NMR measurements can also be used to obtain information about order parameters of solutes in liquid crystal solvents [4,5].

The use of small solutes in liquid crystal solvents has provided a useful route for investigating the intermolecular interactions in these systems. In the past, our group has proposed two important mechanisms for the intermolecular interactions acting between the solute and the liquid crystal molecules. First, the electric quadrupole moment of the solute interacts anisotropically with the average electric field gradient that the solute experiences in the liquid crystal environment. The second mechanism involves short range interactions that depend on the size and shape of the solute $[6,7]$.

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To investigate the short range interactions, it is useful to use systems in which the average electric field gradient is negligibly small. Our group has shown that the molecule $D_{2}$ can be used to measure the average electric field gradients of liquid crystal solvents $[8,9]$. Measurements have been carried out for several nematic liquid crystal solvents including $N$-4-ethoxybenzylidene-4'-n-butylaniline (EBBA) and the mixture Merck ZLI 1132. The signs of the electric field gradients in these two liquid crystal solvents are opposite, and thus a mixture of the two can yield a liquid crystal combination in which the average electric field gradient as seen by the ${ }^{2} \mathrm{H}$ nucleus vanishes. In particular, the measured electric field gradient is zero for a mixture of $55 \mathrm{wt} \% 1132 / \mathrm{EBBA}$ at 301.4 K [8]. Other studies [10] show that the solute methane also experiences an average zero electric field gradient in this mixture. Extensive studies of small and large solutes, including mesogenic molecules such as 1 CB and 5CB, were undertaken to investigate the short range interactions in this mixture [11, 12]. Simple models for the short range interactions were very successful in rationalizing the results obtained [12, 13]. However, it is crucial to ask whether these models are specific for this one special mixture, or whether they provide a reasonable description of the anisotropic short range interactions in nematic liquid crystals in general. Therefore, it would be interesting to examine a series of liquid crystal mixtures in which $\mathrm{D}_{2}$ experiences a zero electric field gradient, and to see to what extent the description of the short range interactions is the same or differs in these mixtures. We shall refer to these special mixtures, in which the measured electric field gradient is zero, as zero efg mixtures. Such mixtures experience a zero efg at a precise temperature; at other temperatures there exists a small non-zero efg. However, we shall see that this small efg does not significantly affect our results. Therefore, throughout this paper, we shall use the term zero efg mixture to include the nematic temperature range of a mixture that exhibits a zero efg at some temperature within this range.

There are several possibilities for investigating zero efg mixtures. One is to use the same combination of liquid crystals such as 1132 and EBBA, but vary the composition. For example, Barnhoorn et al. [14], investigated $56.5 \mathrm{wt} \% 1132 / E B B A$ using $\mathrm{D}_{2}$ as a solute and found that the average electric field gradient is zero at 322 K . Another possibility is to choose a different pair of liquid crystals which have average electric field gradients of opposite sign. As one of the components it would be interesting to use the liquid crystal 5CB (4-n-pentyl-4'-cyanobiphenyl), a relatively simple nematic liquid crystal that has received a lot of experimental and theoretical attention from the NMR community [15-22]. $\mathrm{D}_{2}$ has been used to measure the electric field gradient in this liquid crystal at various temperatures [22]. The magnitude of the average electric field gradient in 5CB is found to be 30 per cent as large as that observed in EBBA, but of opposite sign. This suggests that the electric field gradient should be zero in a mixture of 5 CB and EBBA. A study of $\mathrm{D}_{2}$ dissolved in the liquid crystal mixture $70 \mathrm{wt} \%$ 5CB/EBBA shows that its measured electric field gradient is zero at 316 K [14].

In this paper, the molecule $5 \mathrm{CB}-d_{19}$ (see figure 1) that by itself forms a nematic liquid crystal and is a component of one of the mixtures is studied in the three zero efg mixtures 55 per cent $\dagger 1132 / \mathrm{EBBA}, 56.5$ per cent $1132 / \mathrm{EBBA}$ and 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$. These systems allow us to ignore the electric quadrupole moment-electric field gradient interaction in the mean-field potential. We shall assume that only short range interactions contribute to the anisotropic intermolecular potential in these special mixtures. For our analysis, we shall use two of the simple models for short range

(B) (A)


Figure 1. The coordinate system and atom numbering scheme of the $5 \mathrm{CB}-d_{19}$ molecule.
interactions that were developed $[13,23]$ to explain data on solutes in the $55 \mathrm{wt} \%$ $1132 / E B B A$ mixture. The spectra of $5 \mathrm{CB}-d_{19}$ are not the same in the different mixtures. In this paper we shall demonstrate that the short range potential can be described in the same way in all three mixtures-the spectral differences arise from the differing effects of temperature on the different parts of the potential.

## 2. Review of theory

The solute $5 \mathrm{CB}-d_{19}$ has a rigid ring part and a flexible chain part. According to the RIS approximation [24], each C-C bond has three discrete rotational states: trans, $t$, and two gauche, $g+$ and $g-$. Thus, there are 27 conformer states for 5CB- $d_{19}$. The total energy, $U_{\mathrm{T}, i}(\Omega)$, of conformer $i$ in orientation $\Omega$ is a sum of two terms [25]

$$
\begin{equation*}
U_{\mathrm{T}, i}(\Omega)=U_{\mathrm{int}, i}+U_{i}(\Omega) \tag{1}
\end{equation*}
$$

$U_{\text {int }, i}$, which is assumed to be independent of orientation [26], describes the internal energy of conformer $i . U_{i}(\Omega)$ is an orientation dependent part of the interaction potential. The internal energy, $U_{\text {int }, i}$, is given by

$$
\begin{equation*}
U_{\mathrm{inl}, i}=n_{g} E_{t g}+n_{g+g-}-E_{g+g-}, \tag{2}
\end{equation*}
$$

where $E_{t g}$ is the trans-gauche energy difference, $n_{g}$ is the number of gauche rotations and $n_{g+g-}$ is the number of gauche + followed by gauche - rotations in the conformer. The energy $E_{g+g-}$ is the additional energy required to inhibit successive gauche + gauche - bonds which include large steric interactions. $E_{g+g-}$ is taken as $1.5 \mathrm{kcal} \mathrm{mol}^{-1}$ [12]. The probability of conformer $i, p_{i}$, is given by

$$
\begin{equation*}
p_{i}=\frac{\exp \left(\frac{-U_{\mathrm{int}, i}}{k T}\right) \int \exp \left(\frac{-U_{i}(\Omega)}{k T}\right) d \Omega}{\sum_{i} \exp \left(\frac{-U_{\mathrm{in}, i, i}}{k T}\right) \int \exp \left(\frac{-U_{i}(\Omega)}{k T}\right) d \Omega} \tag{3}
\end{equation*}
$$

where the integration is over all orientations $\Omega$. For a nematic liquid crystal with the director aligned parallel to the magnetic field direction, the quadrupolar splitting of a deuteron in conformer $i, v_{Q, i}$, is given by

$$
\begin{equation*}
v_{Q, i}=\sum_{\alpha} \sum_{\beta} \frac{e^{2} Q}{h} q_{\alpha \beta, i} S_{\alpha \beta, i} \tag{4}
\end{equation*}
$$

where $e Q$ is the quadrupole moment of the ${ }^{2} \mathrm{H}$ nucleus, $S_{\alpha \beta, i}$ and $q_{\alpha \beta, i}$ are the $\alpha \beta$
components of the order matrix and the electric field gradient of the deuteron nucleus in a conformer coordinate frame. The components of the order matrix for conformer $i, S_{\alpha \beta, i}$, are given by

$$
\begin{equation*}
S_{\alpha \beta, i}=\frac{\int\left(3 \cos \theta_{\alpha} \cos \theta_{\beta}-\delta_{\alpha \beta}\right) \exp \left(\frac{-U_{i}(\Omega)}{k T}\right) d \Omega}{2 \int \exp \left(\frac{-U_{i}(\Omega)}{k T}\right) d \Omega}, \tag{5}
\end{equation*}
$$

where $\cos \theta_{\alpha}, \cos \theta_{\beta}$ are the direction cosines of the $\alpha, \beta$ axes with respect to the $Z$, director, axis. The calculated quadrupolar splitting, $\Delta v_{Q}$, is then

$$
\begin{equation*}
\Delta v_{Q}=\sum_{i} v_{Q, i} p_{i} \tag{6}
\end{equation*}
$$

The principal axes, $a, b, c$, of the intramolecular electric field gradient tensor of the ring deuterons have axis $b$ along the $\mathrm{C}-\mathrm{D}$ bond and axis $a$ in the plane of the ring. The quadrupolar splitting of conformer $i, v_{Q, i}$, is then written in terms of the quadrupolar coupling constant, $e^{2} Q q_{b b} / h$, and the asymmetry parameter, $\eta=\left(q_{a a}-q_{c c}\right) / q_{b b}$. The quadrupolar coupling constant for ring deuterons is 185 kHz , and $\eta$ is 0.04 [12]. For the flexible chain part, the quadrupolar coupling constant is taken as 168 kHz and $\eta$ is taken as zero [12].

In order to calculate the quantities $p_{i}, S_{\alpha \beta, i}$ and hence $\Delta v_{Q}$, information about both the $U_{i}(\Omega)$ and $U_{\text {int, }, i}$ is necessary. According to [6], the interaction potential, $U_{i}(\Omega)$, can be written as a sum of the electric field gradient-electric quadrupole moment interaction potential and a short range interaction potential, $U_{\mathrm{sr}, i}(\Omega)$. In zero electric field gradient mixtures, the interaction potential, $U_{i}(\Omega)$, is assumed to be equal to the short range potential, $U_{\mathrm{st}, i}(\Omega)$. Since the nature of the short range potential is not known exactly, we shall use models for it. These will be reviewed in the Discussion section.

## 3. Experimental

The liquid crystal ZLI 1132, which is a eutectic mixture of alkylcyclohexylcyanobenzenes and alkylcyclohexylcyanobiphenyls, was purchased from E. Merck, Darmstadt and was not purified prior to use. The liquid crystal EBBA was synthesized in Amsterdam using the procedure given in [27]. The liquid crystal 5CB was purchased from Merck Ltd, U.K. The liquid crystals 1132, EBBA and 5CB were used to prepare the liquid crystal mixtures $70 \mathrm{wt} \%$ 5CB/EBBA, $55 \mathrm{wt} \% 1132 / \mathrm{EBBA}$ and $56.5 \mathrm{wt} \%$ $1132 / E B B A$. The solute 5CB- $d_{19}$ was synthesized at UBC [12]. 1-2 wt $\%$ of 5CB- $d_{19}$ as solute was dissolved in each liquid crystal mixture, the mixture heated to the isotropic phase, and mixed using a vortex stirrer. The sample was subjected to freeze-pump-thaw cycles until no gas evolved from the liquid crystal mixture. The samples were transferred to NMR tubes, and the tubes were flame sealed under vacuum. Quadrupolar echo excitation was used to run the NMR experiment on a Bruker CXP-200 NMR spectrometer operating at 30.76 MHz for ${ }^{2} \mathrm{H}$ nuclei. Spectra were obtained by Fourier transforming from the top of the echo [28]. The experiment was repeated as a function of temperature from the solid to the isotropic phase region for all three liquid crystal mixtures.

Separate microscope slides were prepared from the pure solvents 55 per cent $1132 / E B B A$ and 70 per cent 5CB/EBBA, and were studied using a Leitz Laborlux 12POL polarizing microscope equipped with a Mettler FP2 heating stage by Dr Mary E. Neubert at Kent State University to determine the phase transitions of
these zero efg mixtures. It was found that $T_{\mathrm{N}}$, the nematic-isotropic transition temperature, of 55 per cent $1132 / \mathrm{EBBA}$ is in the range 341.8 K to 342.4 K , and that $T_{\mathrm{NI}}$ of 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ is in the range 320.6 K to 321.4 K . It was also found that all three liquid crystal mixtures used in this study are in the nematic phase over the temperature range used for the NMR experiments.

## 4. Results

The NMR spectrum of $5 \mathrm{CB}-d_{19}$ in zero efg solvents has seven pairs of quadrupolar lines, each pair corresponding to a different C-D bond site. Figure 2 shows the spectra of $5 \mathrm{CB}-d_{19}$ in 55 per cent $1132 /$ EBBA at 307.1 K and in 70 per cent 5 CB/EBBA at 306.8 K . The quadrupolar lines are broadened due to the dipole-dipole coupling between deuterons. Quadrupolar splittings were measured in a manner consistent with line shape simulations. Measurements were carried out at temperatures ranging from 250 K to the isotropic temperature on the mixtures 55 per cent $1132 / \mathrm{EBBA}, 70$ per cent $5 \mathrm{CB} / \mathrm{EBBA}$ and 56.5 per cent $1132 / \mathrm{EBBA}$. Measured line positions are tabulated in tables 1 to 3. Spectral line assignments were based on previous work [29] and are in agreement with predictions from our calculations below.

As the temperature approaches $T_{\mathrm{NI}}$, the spectra begin to appear as a superposition of nematic and isotropic peaks. The lowest temperature at which the isotropic peak appears is taken to be $T_{\mathrm{NI}}$. The $T_{\mathrm{NI}}$ of 55 per cent $1132 / \mathrm{EBBA}$ and 56.5 per cent $1132 / \mathrm{EBBA}$ are 337 K and 339 K , respectively, and the $T_{\mathrm{NI}}$ of 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ is 316 K . These numbers differ slightly from those above because the samples used for NMR contain deuteriated materials.

The measured quadrupolar splittings at position $1, \Delta v_{1}$, are plotted against temperature in figure 3 . The curves corresponding to 55 per cent $1132 /$ EBBA and 56.5 per cent $1132 / \mathrm{EBBA}$ are similar. However, the curve corresponding to the mixture 70 per cent $5 \mathrm{CB} /$ EBBA appears to have a break at 307 K (see figure 3). Below this temperature the quadrupolar splitting changes linearly with temperature. However, the microscope study indicates that there is no phase transition taking place near 307 K in this mixture. Thus, the liquid crystal mixtures are nematic for all points given in figure 3.

## 5. Discussion

### 5.1. General

The purpose of this paper is to examine several zero efg mixtures and to investigate the short range potentials in these mixtures. In addition we shall investigate to what extent the description of the anisotropic short range potential is similar or is different in the various mixtures. One way of emphasizing small differences among the zero efg mixtures is to plot ratios of the quadrupolar splittings, such as $\Delta v_{s} / \Delta v_{1}$, against $\Delta v_{1}$. These plots shall be referred to as ratio plots. Ratio plots for 5 CB- $d_{19}$ were previously used to illustrate differences among the liquid crystals 1132, EBBA, 5CB and 55 per cent $1132 / E B B A$ [12]. In that study, the differences were ascribed to the presence of a non-zero electric field gradient in the various liquid crystals.

A plot of $\Delta v_{5} / \Delta v_{1}$ against $\Delta v_{1}$ is shown in figure 4. Intuitively, one might expect that ratio plots for all zero efg mixtures would be similar. However, the differences between 55 per cent 1132/EBBA and 70 per cent 5CB/EBBA are large and comparable to those between the liquid crystals 1132 and EBBA in [12]. On the other hand, the ratio plots of $5 \mathrm{CB}-d_{19}$ in 55 per cent $1132 / \mathrm{EBBA}$ and in 56.5 per cent $1132 / \mathrm{EBBA}$ are


Figure 2. Experimental ${ }^{2} \mathrm{H}-\mathrm{NMR}$ spectra of $5 \mathrm{CB}-d_{19}$ dissolved in the zero efg mixtures 55 per cent $1132 / \mathrm{EBBA}$, at 307.1 K , and 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ at 306.8 K .

Table 1. Quadrupolar splittings (in kHz ) of $5 \mathrm{CB}-d_{19}$ in 55 per cent $1132 / \mathrm{EBBA}$.

| Temperature $/ \mathrm{K}$ | $\Delta v_{1}$ | $\Delta v_{2}$ | $\Delta v_{3}$ | $\Delta v_{4}$ | $\Delta v_{5}$ | Ring $A$ | Ring $B$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 251.4 | 77.782 | 63.768 | 65.233 | 49.559 | 35.790 | 21.728 | 17.577 |
| 256.1 | 77.050 | 62.255 | 63.719 | 47.899 | 34.569 | 21.435 | 17.430 |
| 261.1 | 75.878 | 60.887 | 62.597 | 46.142 | 33.446 | 21.240 | 17.236 |
| 265.3 | 75.048 | 59.569 | 61.327 | 44.823 | 32.568 | 20.946 | 17.040 |
| 270.7 | 74.267 | 58.251 | 59.960 | 43.066 | 31.396 | 20.946 | 16.893 |
| 275.8 | 73.974 | 57.177 | 58.739 | 41.747 | 30.663 | 20.702 | 16.699 |
| 281.5 | 72.314 | 55.028 | 56.688 | 39.745 | 29.199 | 20.263 | 16.161 |
| 285.3 | 70.898 | 53.319 | 55.077 | 38.329 | 28.173 | 19.725 | 15.721 |
| 292.1 | 68.309 | 50.438 | 52.489 | 35.936 | 26.366 | 18.896 | 14.941 |
| 296.4 | 66.796 | 48.730 | 50.634 | 34.520 | 25.292 | 18.310 | 14.501 |
| 302.1 | 64.697 | 46.337 | 48.339 | 32.616 | 23.827 | 17.577 | 13.818 |
| 307.1 | 62.743 | 44.189 | 46.239 | 30.858 | 22.606 | 16.698 | 13.232 |
| 312.7 | 59.911 | 41.308 | 43.456 | 28.612 | 20.995 | 15.770 | 12.352 |
| 317.0 | 57.079 | 38.768 | 41.014 | 26.757 | 19.579 | 14.843 | 11.572 |
| 323.1 | 53.368 | 35.448 | 37.646 | 24.218 | 17.724 | 13.524 | 10.497 |
| 327.0 | 49.316 | 32.079 | 34.276 | 21.776 | 15.917 | 12.255 | 9.325 |
| 332.6 | 42.333 | 26.806 | 28.661 | 18.017 | 13.182 | 10.156 | 7.567 |
| 334.6 | 36.622 | 24.315 | 25.927 | 16.307 | 11.962 | 9.130 | 6.786 |

Table 2. Quadrupolar splittings (in kHz ) of $5 \mathrm{CB}-d_{19}$ in 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$.

| Temperature/K | $\Delta v_{1}$ | $\Delta v_{2}$ | $\Delta v_{3}$ | $\Delta v_{4}$ | $\Delta v_{5}$ | Ring $A$ | Ring $B$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 251.9 | 72.509 | 57.812 | 59.569 | 44.140 | 32.031 | 19.725 | 15.966 |
| 255.9 | 70.702 | 55.663 | 57.958 | 42.626 | 30.956 | 19.189 | 15.526 |
| 261.2 | 69.579 | 53.564 | 55.712 | 40.233 | 29.345 | 18.652 | 14.940 |
| 265.3 | 68.163 | 52.148 | 54.101 | 38.720 | 28.271 | 18.212 | 14.550 |
| 271.1 | 65.868 | 49.511 | 51.513 | 36.230 | 26.513 | 17.528 | 13.963 |
| 276.1 | 64.550 | 47.704 | 49.755 | 34.569 | 25.438 | 17.040 | 13.524 |
| 281.9 | 62.108 | 44.921 | 46.972 | 32.177 | 23.827 | 16.258 | 12.841 |
| 285.9 | 60.399 | 43.017 | 45.116 | 30.517 | 22.704 | 15.721 | 12.352 |
| 292.1 | 57.861 | 40.331 | 42.626 | 28.319 | 21.044 | 15.038 | 11.766 |
| 296.6 | 56.298 | 38.671 | 40.819 | 26.854 | 20.018 | 14.452 | 11.425 |
| 302.0 | 53.906 | 36.620 | 38.573 | 24.999 | 18.700 | 13.866 | 10.937 |
| 306.8 | 51.563 | 34.570 | 36.524 | 23.438 | 17.480 | 13.232 | 10.400 |
| 308.8 | 49.462 | 32.909 | 34.813 | 22.118 | 16.551 | 12.597 | 9.764 |
| 310.8 | 46.728 | 30.859 | 32.714 | 20.702 | 15.477 | 11.816 | 9.130 |
| 312.7 | 42.968 | 28.026 | 29.736 | 18.700 | 14.013 | 10.595 | 8.153 |
| 313.7 | 40.624 | 24.464 | 28.075 | 17.578 | 13.134 | 10.008 | 7.616 |
| 314.7 | 37.646 | 24.608 | 25.976 | 16.210 | 12.059 | 9.228 | 6.982 |
| 315.7 | 34.130 | 21.678 | 22.704 | 14.404 | 10.839 | 8.104 | 6.201 |

Table 3. Quadrupolar splittings (in kHz ) of $5 \mathrm{CB}-d_{19}$ in 56.5 per cent $1132 / \mathrm{EBBA}$.

| Temperature/K | $\Delta v_{1}$ | $\Delta v_{2}$ | $\Delta v_{3}$ | $\Delta v_{4}$ | $\Delta v_{5}$ | Ring $A$ | Ring $B$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 261.4 | 75.927 | 61.156 | 62.987 | 46.569 | 33.691 | 21.239 | 17.211 |
| $266 \cdot 1$ | 75.255 | 59.997 | 61.827 | 45.349 | 32.714 | 20.995 | 16.966 |
| 271.7 | 74.340 | 58.287 | 60.180 | 43.334 | 31.616 | 20.812 | 16.783 |
| 276.0 | 73.791 | 57.311 | 59.143 | 42.236 | 30.821 | 20.751 | 16.722 |
| 281.9 | 72.630 | 55.480 | 57.067 | 40.160 | 29.479 | 20.201 | 16.234 |
| $286 \cdot 1$ | 71.044 | 53.649 | 55.541 | 38.695 | 28.441 | 19.713 | 15.929 |
| 292.5 | 69.029 | 50.963 | 53.222 | 36.620 | 26.854 | 19.042 | 15.075 |
| 296.7 | 67.321 | 49.133 | 51.390 | 35.095 | 25.634 | 18.432 | 14.587 |
| 302.0 | 65.123 | 46.813 | 48.889 | 33.080 | 24.169 | 17.638 | 13.915 |
| $307 \cdot 1$ | 63.415 | 44.615 | 46.752 | 31.372 | 22.887 | 16.844 | 13.304 |
| 31.6 | 60.851 | 41.870 | 44.249 | 29.235 | 21.362 | 15.990 | 12.511 |
| 317.1 | 58.226 | 39.489 | 41.869 | 27.403 | 20.018 | 15.075 | 11.718 |
| 323.1 | 54.686 | 36.376 | 38.513 | 24.963 | 18.249 | 13.854 | 10.742 |
| 327.6 | 50.963 | 33.263 | 35.522 | 22.704 | 16.600 | 12.633 | 9.764 |
| 328.6 | 50.109 | 32.653 | 34.972 | 22.277 | 16.234 | 12.389 | 9.459 |
| 330.1 | 48.095 | 31.127 | 33.202 | 21.117 | 15.380 | 11.779 | 8.971 |
| 330.6 | 47.057 | 30.089 | 32.226 | 20.446 | 14.892 | 11.413 | 8.666 |
| 332.6 | 44.799 | 28.502 | 30.517 | 19.286 | 14.037 | 10.802 | 8.056 |
| 333.6 | 43.578 | 27.648 | 29.601 | 18.676 | 13.610 | 10.436 | 7.812 |
| 334.6 | 42.296 | 26.732 | 28.747 | 18.065 | 13.183 | 10.070 | 7.507 |
| $335 \cdot 1$ | 40.526 | 25.573 | 27.465 | 17.272 | 12.572 | 9.642 | 7.140 |
| 336.1 | 38.207 | 23.864 | 25.817 | 16.112 | 11.718 | 8.971 | 6.591 |
| 337.1 | 36.193 | 22.460 | 23.925 | 15.075 | 11.046 | 8.300 | 6.163 |
| 338.1 | 33.019 | 20.263 | 21.422 | 13.732 | 10.009 | 7.446 | 5.553 |



Figure 3. The quadrupolar splitting $\Delta v_{1}$ versus temperature for the mixtures 55 per cent $1132 / \mathrm{EBBA}, 70$ per cent $5 \mathrm{CB} / \mathrm{EBBA}$ and 56.5 per cent $1132 /$ EBBA.


Figure 4. Quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ versus $\Delta v_{1}$ of $5 \mathrm{CB}-d_{19}$ in the zero efg mixtures 55 per cent $1132 / \mathrm{EBBA}, 70$ per cent $5 \mathrm{CB} / \mathrm{EBBA}$ and 56.5 per cent $1132 / \mathrm{EBBA}$.
superimposable. This latter fact allows us to evaluate the effect of a small residual electric field gradient present in the mixtures 55 per cent $1132 / \mathrm{EBBA}$ and 56.5 per cent $1132 / \mathrm{EBBA}$ at temperatures other than 301.4 K and 322 K where the electric field gradient is zero.

In such zero efg mixtures, the average electric field gradient measured using $\mathrm{D}_{2}$ changes sign and magnitude with changing temperature. At any given temperature, the average electric field gradient in the 55 per cent 1132/EBBA mixture differs from that in the 56.5 per cent $1132 / E B B A$ mixture. If these small efg's made a significant contribution to the anisotropic orientational potential, the ${ }^{2} \mathrm{H}$ spectra of $5 \mathrm{CB}-d_{19}$ should differ between the two mixtures. However, the ratio plots in figure 4 show that the quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ are identical for the two mixtures over the temperature range $250-337 \mathrm{~K}$. This result, together with the equivalence of the $\Delta v_{1}$ for the two 1132 /EBBA mixtures in figure 3 , shows that the small electric field gradients present in these mixtures have a negligible effect on the spectra. The quadrupole moment-electric field gradient mechanism can be neglected as an important orientational mechanism in these mixtures. Thus, when we refer to a zero efg mixture, we include the entire nematic range of a mixture that has a precisely zero efg at one specific temperature. Note that van der Est et al. [30], have reported a quantitative temperature and concentration dependence study of the efg in 1132/EBBA mixtures.

We shall also assume that the contribution of the electric field gradient-electric quadrupole moment interaction to $U_{\mathrm{T}, i}(\Omega)$ is negligible throughout the nematic range of the zero efg mixture 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$. Thus the differences in figure 4 between 70 per cent 5CB/EBBA and the other zero efg mixtures do not arise from the electric field gradient-molecular quadrupole moment mechanism. Do these differences imply that the details of the short range potential are liquid crystal dependent? We shall attempt to answer this question below.

To proceed, it is useful to introduce a model for the short range potential, $U_{\mathrm{sr}, i}(\Omega)$. It seems sensible to choose a model that provides a successful fit to the orientational order parameters measured for a range of rigid solutes in a zero efg nematic solvent [7, 13,23]. However, the internal motions in 5CB add extra complexity to the problem. It does not help that literature values of $E_{t g}$ for butane vary from 400 to $900 \mathrm{cal} \mathrm{mol}^{-1}$ [24,31-37]. Because we wish to draw meaningful conclusions from our work, we shall investigate two different models for the short range potential in an attempt to come up with a comparison among mixtures that is independent, as far as possible, of the model chosen. Since no significant differences between the zero efg mixtures 55 per cent 1132/EBBA and 56.5 per cent $1132 /$ EBBA are observed, only the zero efg mixtures 55 per cent $1132 /$ EBBA and 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ shall be compared in the following sections.

### 5.2. CZ model

Van der Est et al. [6], introduced the short range potential, $U_{\mathrm{sr}}(\Omega)$,

$$
\begin{equation*}
U_{\mathrm{sr}}(\Omega)=\frac{1}{2} k C(\Omega)^{2} \tag{7}
\end{equation*}
$$

to calculate order parameters of small solutes in the zero efg mixture 55 per cent 1132/EBBA. In equation (7), $C$ is the circumference of the solute projected on to a plane perpendicular to the director, and $k$, a model parameter, is a property of the liquid crystal. In this model, the liquid crystal is treated as an elastic continuum. The solute is described as a collection of van der Waals spheres.

The order parameters recalculated from a one parameter fit of $k$ in equation (7) to

46 solutes of varying symmetry agree well with the experimental order parameters [13,23]. However, if the fit is done for individual solutes, the parameter $k$ is consistently smaller for larger solutes such as 2,4-hexadiyne, 1 CB and 5CB than for smaller ones. Consequently, Zimmerman et al. [13], introduced an additional term into the short range potential, $U_{\mathrm{sr}}(\Omega)$, which yielded an excellent and consistent fit for large as well as small solutes in the zero efg mixture 55 per cent $1132 / E B B A$. The modified short range potential is written

$$
\begin{equation*}
U_{\mathrm{sr}}(\Omega)=\frac{1}{2} k_{z} C(\Omega)^{2}+\frac{1}{2} k_{x y} Z(\Omega) C(\Omega), \tag{8}
\end{equation*}
$$

where $k_{z}$ and $k_{x y}$ are the model parameters. If the solute is considered as a cylinder, then equation (8) has the form of an anisotropic surface interaction. $Z(\Omega)$ is the maximum length of the solute, described as a collection of van der Waals spheres, projected on to the director direction for solute orientation $\Omega$. Equation (8) can be rewritten in terms of the model parameters $k_{z}$ and $\xi$,

$$
\begin{equation*}
U_{\mathrm{sr}}(\Omega)=\frac{1}{2} k_{z} C(\Omega)^{2}+\frac{1}{2} k_{z} \xi Z(\Omega) C(\Omega), \tag{9}
\end{equation*}
$$

where $\xi=k_{x y} / k_{z}$ is dimensionless. Calculations using equation (8) or (9) for the short range potential shall be referred to as CZ model calculations in this paper. In the notation $C Z$, the ' $C$ ' refers to the $C(\Omega)$ term in equations ( 8 ) and (9), and the ' $Z$ ' to the $Z(\Omega)$ term.

### 5.3. CI model

In an attempt to introduce a better model for the anisotropic short range interaction between the solute surface and the liquid crystal, Zimmerman et al. [23], suggested that the short range potential can be written

$$
\begin{equation*}
U_{\mathrm{sr}}(\Omega)=\frac{1}{2} k C(\Omega)^{2}+\frac{1}{2} k_{\mathrm{s}} \int C_{\mathrm{Z}}(\Omega) d Z \tag{10}
\end{equation*}
$$

where k and $k_{\mathrm{s}}$ are the model parameters, and $\mathrm{C}_{\mathrm{Z}}(\Omega)$ is the circumference of the solute at distance $Z$. The second term in equation (10) models an anisotropic interaction between the solute surface and the liquid crystal. The first term, as in the case of van der Est et al. [6], accounts for the elastic distortion of the liquid crystal. This model gave the best fit to the experimental order parameters of 46 solutes in 55 per cent $1132 / \mathrm{EBBA}$. Equation (10) can be rewritten in terms of the model parameters $k_{\mathrm{s}}$ and $\xi^{\prime}$ as

$$
\begin{equation*}
U_{\mathrm{sr}}(\Omega)=\frac{1}{2} k_{\mathrm{s}} \xi^{\prime} C(\Omega)^{2}+\frac{1}{2} k_{\mathrm{s}} \int C_{\mathrm{Z}}(\Omega) d Z \tag{11}
\end{equation*}
$$

where $\xi^{\prime}=k / k_{\mathrm{s}}$ is dimensionless. The calculations using equation (10) or (11) for the short range potential shall be referred to in this paper as CI model calculations. In the notation CI , the ' C ' refers to the $C(\Omega)$ term in equations (10 and (11), and the ' T ' to the integral term.

### 5.4. RIS parameter and molecular geometry

One of the complexities of the $5 \mathrm{CB}-d_{19}$ molecule is the presence of the flexible hydrocarbon chain which introduces the additional parameter, $E_{t g}$, the trans-gauche energy difference. Since $E_{t g}$ is an intramolecular property, it should be independent of temperature and environment. $E_{t g}$ values have been measured for $n$-butane in isotropic solvents and it would seem reasonable to use these values for 5 CB- $d_{19}$ in zero efg mixtures. Most of the literature values of liquid $n$-butane are close to $500 \mathrm{cal} \mathrm{mol}^{-1}$
[33-36]. However, one study [32] reports a value of $966 \mathrm{cal} \mathrm{mol}^{-1}$ for gaseous $n$-butane. Since there are a range of $E_{t g}$ values in the literature, we shall explore calculations using $E_{t g}$ values of 500,700 and $900 \mathrm{cal} \mathrm{mol}^{-1}$.

In addition, the geometry of $5 \mathrm{CB}-d_{19}$ must be known in order to calculate the quadrupolar splittings. The parameters $C$ and $Z$ in the equations for $U_{\mathrm{sr}}(\Omega)$ depend on the bond lengths, and the quadrupolar splittings depend on the bond angles. We assume that the benzene rings are regular hexagonal, and that the angle between the normals to the two benzene rings is $30^{\circ}$ [17]. In addition, we assume that all the methylene groups are described by the CCC and CCD bond angles $112.5^{\circ}$ and $108.82^{\circ}$. The DCD plane in each $\mathrm{CD}_{2}$ group is assumed to bisect the CCC angle. The dihedral angle for a trans-gauche conformational change is $112.0^{\circ}$.

Two additional unknowns in the molecular geometry of 5CB- $d_{19}$ are the angles $\theta^{\prime}$ (see figure 1) and $\theta_{\mathrm{d}}$, where $\theta_{\mathrm{d}}$ is the dihedral angle between the $\mathrm{C}_{1} \mathrm{C}_{2}$ bond and the plane of benzene ring $A$. Most studies of 5 CB assume that the angle $\theta^{\prime}$ is $120^{\circ}$. However, Photinos et al. [15], used the value $124^{\circ}$ from X-ray studies on 5OCB for their calculations of $n \mathrm{CB}$ and $n \mathrm{OCB}$ liquid crystals. While 50 CB and 5 CB will have different geometries, it nevertheless seems worthwhile to explore the possibility of a value of $\theta^{\prime}$ different from $120^{\circ}$ for 5 CB . Of the many possibilities, we performed four different calculations corresponding to four different geometries: the four geometries are (1) $\theta^{\prime}=120^{\circ}, \theta_{\mathrm{d}}=0^{\circ}$ (the bond $\mathrm{C}_{1} \mathrm{C}_{2}$ is coplanar to the benzene ring $A$-this geometry shall be referred to as PL-0; (2) $\theta^{\prime}=124^{\circ}, \theta_{d}=0^{\circ}$ (this geometry shall be referred to as PL-4); (3) $\theta^{\prime}=120^{\circ}, \theta_{\mathrm{d}}=90^{\circ}$ (the ring- $\mathrm{C}_{1}$ bond lies along the para-axis of ring $A$ and the bond $\mathrm{C}_{1} \mathrm{C}_{2}$ is perpendicular to the benzene ring $A$-this geometry shall be referred to as PERP-0); (4) $\theta^{\prime}=124^{\circ}, \theta_{d}=90^{\circ}$ (starting from the PL-4 geometry, the hydrocarbon chain is rotated $90^{\circ}$ about the para-axis of ring $A$-this geometry shall be referred to as PERP-4).

### 5.5. Individual fit model parameters

A least squares minimization routine was used to obtain best fit model parameters for each experimental spectrum from a minimization of the differences between experimental and calculated quadrupolar splittings of $5 \mathrm{CB}-d_{19}$ as solute in the zero efg

Table 4. Fitted ranges for $\theta$ of 5 CB (see figure 1) in 55 per cent 1132/EBBA and 70 per cent 5CB/EBBA.

| Model and geometry | $E_{t g} / \mathrm{cal} \mathrm{mol}^{-1}$ | $\theta / \mathrm{deg}$ of 55 per cent $1132 / \mathrm{EBBA}$ | $\theta / \mathrm{deg}$ of 70 per cent 5CB/EBBA |
| :---: | :---: | :---: | :---: |
| COZ | 500 | 118.88-117.48 | 118.70-117.48 |
|  | 700 | 118.96-117.90 | 118.80-118.00 |
| PERP-0 | 900 | 119.02-118.28 | 118.90-118.44 |
| COZ | 500 | 119.00-117.48 | 118.80-117.48 |
|  | 700 | 119.14-118.04 | 118.96-118.18 |
| PERP-4 | 900 | 119.26-118.58 | 119.14-118.78 |
| CAI | 500 | 119.76-122.20 | 119.94-122.68 |
|  | 700 | 119.60-121.00 | 119.72-121.06 |
| PERP-0 | 900 | 119.38-119.52 | 119.42-119.00 |
| CAI | 500 | 120.38-123.26 | 120.62-123.82 |
|  | 700 | 120.18-121.88 | 120.34-122.00 |
| PERP-4 | 900 | 119.88-120.12 | 119.90-120.04 |


(a)

(b)


Figure 5. (a) RMS (root mean squares deviation) versus temperature of the fits to individual spectra of 5 CB in 55 per cent $1132 / E B B A$ for the different geometries PL-0, PL-4, PERP-0 and PERP-4. Open symbols are used for the $C Z$ model with $E_{t g}$ equal to $500 \mathrm{cal} \mathrm{mol}^{-1}$. Closed symbols are used for the CI model with $E_{t g}$ equal to $500 \mathrm{cal} \mathrm{mol}^{-1}$. (b) the same as (a) for $E_{t g}=700 \mathrm{cal} \mathrm{mol}^{-1}$. (c) the same as (a) for $E_{f g}=900 \mathrm{cal} \mathrm{mol}^{-1}$.
mixtures 55 per cent 1132/EBBA and 70 per cent 5 CB/EBBA. The quality of the fit is judged mainly from RMS (root mean square deviation) values, i.e. the lower the RMS the better the quality of the fit. We find that the quality of the fit depends on the parameters $\theta$ (see figure 1) and $E_{t g}$. When the angle $\theta$ was varied, the calculated quadrupolar splittings agreed very well with the experimental quadrupolar splittings at the ring positions. However, the variation of $\theta$ did not change much the calculated quadrupolar splittings at the chain positions. Hoatson et al. [12], also allowed $\theta$ to vary and obtained a good fit for the ring deuterons in their study of $5 \mathrm{CB}-d_{19}$ in liquid crystals. When the parameter $E_{t g}$ was varied for each individual temperature, the best fit was obtained for $E_{t g}$ values as low as $500 \mathrm{cal} \mathrm{mol}^{-1}$. However, the fitted $E_{t g}$ values varied with temperature. This contradicts the fact that the intramolecular property $E_{t g}$ should be independent of temperature. Therefore, we decided to fix the parameter $E_{t g}$ to certain values, 500,700 and $900 \mathrm{cal} \mathrm{mol}^{-1}$, at all temperatures. These values span the range of literature $E_{t g}$ values [24,31-37].

Separate calculations were performed for both the CZ and CI models for the four geometries PL-0, PL-4, PERP-0 and PERP-4 and for the three $E_{t g}$ values 500, 700 and $900 \mathrm{cal} \mathrm{mol}^{-1}$. The model parameters $k_{z}, k_{x y}$ and $\theta$ were fitted in the CZ model calculations. The CI model calculation gives $k, k_{\mathrm{s}}$ and $\theta$ values. Therefore, we obtain 12 sets of ( $k_{2}, k_{x y}, \theta$ ) and of ( $k, k_{\mathrm{s}}, \theta$ ) values for each spectrum. The fitted $\theta$ value ranges are reported in table 4. The $\theta$ values obtained are consistent with the value reported in [29]. In order to reduce the number of possible calculations in the following, we shall examine the quality of these fits and choose one set of $k_{z}, k_{x y}$ and one set of $k, k_{\mathrm{s}}$ values. We shall choose the geometry and $E_{t g}$ values that fit best the experimental quadrupolar
splittings as the most appropriate basis for comparison of the real intermolecular potential between mixtures.

The quality of the fit (RMS) to the 55 per cent 1132/EBBA mixture for the four different geometries using the two different models and three different $E_{t g}$ values is shown in figure 5 . While some fits are obviously much better than others, most of these fits are acceptable considering the many assumptions involved in the modelling process. It is unfortunate that the parameters are correlated such that it is not possible to choose a definitive value of $E_{t g}$ from these calculations. However, calculations that use a value of $E_{t g}$ of the order $500 \mathrm{cal} \mathrm{mol}^{-1}$ are generally considered preferable [15]. In all cases for the CI model, the PERP-4 geometry gives the best fit. For the CZ model, the PERP-0 geometry gives the best fit except for $E_{t g}$ of $900 \mathrm{cal} \mathrm{mol}^{-1}$ at low temperatures, where the PERP-4 geometry gives the best fit. Similar results were obtained for the 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ mixture. Based of these plots, we decided to choose the PERP-0 geometry for the CZ model and the PERP-4 geometry for the CI model. Henceforth, whenever we refer to CZ model parameters, it implies that the parameters are calculated with the CZ model using the PERP-0 geometry. Similarly, any reference to the CI model parameters implies that the parameters are calculated with the CI model using the PERP-4 geometry.

### 5.5.1. Temperature dependence of individual fit model parameters

The temperature dependence of the short page potential is described by the temperature dependence of the CZ and CI model parameters. We use the parameters $k_{z}$ and $k_{\mathrm{s}}$ to characterize the magnitude of the short range potentials. The parameters $\xi$ and $\xi^{\prime}$ are ratios of model parameters. If all contributions to the potential scale the same way with temperature, these ratios would be independent of temperature. First, we shall analyse the temperature dependence of the model parameters $k_{z}$ and $k_{\mathrm{s}}$. Then, we shall examine the temperature dependence of the ratios $\xi$ and $\xi^{\prime}$.

### 5.5.2. $k_{z}$ and $k_{\mathrm{s}}$

Our main interest here is to see how the model parameters $k_{\mathrm{z}}$ and $k_{\mathrm{s}}$ depend on factors such as liquid crystal mixture, $E_{t g}$ and temperature. The fitted $k_{z}$ and $k_{\mathrm{s}}$ values obtained for each experimental temperature and for $E_{t g}$ of 500,700 and $900 \mathrm{cal} \mathrm{mol}^{-1}$ are plotted as reduced model parameters, $k_{i} / T$, against reduced temperature, $T_{\mathrm{r}}=T / T_{\mathrm{N}}$, in figure 6 . We use reduced model parameters because in the calculation of quadrupolar splittings the $k_{i}$ are always divided by temperature; we use reduced temperature because the liquid crystal mixtures 55 per cent $1132 / \mathrm{EBBA}$ and 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ have different $T_{\mathrm{NI}}$ values.

As temperature increases towards $T_{\mathrm{N}}$, the reduced model parameters decrease. The $k_{z} / T$ values of 55 per cent $1132 /$ EBBA are higher than those of 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ at reduced temperatures less than 0.95 , and this is true for all three $E_{t g}$ values. The $k_{s} / T$ values are quite similar in both mixtures. However, the break observed in figure 3 for the 70 per cent 5CB/EBBA mixture is also apparent in figure 6.

### 5.5.3. $\xi$ and $\xi^{\prime}$

The ratios $\xi$ and $\xi^{\prime}$ are plotted against reduced temperature in figure 7 . The similar results obtained for both samples, independent of model used, is striking. Thus the form of the short range potential appears to be the same in both mixtures.

The temperature dependence of $\xi$ depends on $E_{t g}$. The ratio $\xi$ has a large temperature dependence for the $E_{t g}$ value $500 \mathrm{cal} \mathrm{mol}^{-1}$, is less dependent on temperature for the


Figure 6. (a) The reduced model parameter $k_{i} / T$ (CZ model, PERP-0 geometry) versus reduced temperature. Different symbols represent the $k_{z} / T$ values of 70 per cent 5CB/EBBA (open symbols) and 55 per cent $1132 /$ EBBA (filled symbols) for different $E_{\text {tg }}$ values as indicated. (b) the reduced model parameter $k_{\mathrm{s}} / T$ (CI model, PERP-4 geometry) versus reduced temperature. The symbols have the same meaning as in (a).


Figure 7. (a) The ratio $\xi$ (CZ model, PERP-0 geometry) versus reduced temperature for 5CB Different symbols represent the $\xi$ values of 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ (open symbols) and 55 per cent $1132 / \mathrm{EBBA}$ (filled symbols) for different $E_{t g}$ values as indicated. (b) Ratio $\xi^{\prime}$ (CI model, PERP-4 geometry) versus reduced temperature. The symbols have the same meaning as in (a).
$E_{t g}$ value $700 \mathrm{calmol}^{-1}$, and is almost independent of temperature for the $E_{t g}$ value $900 \mathrm{cal} \mathrm{mol}^{-1}$. On the other hand, the ratio $\xi^{\prime}$ is small and has no significant temperature dependence for all $E_{t g}$ values. Except for the CZ calculations at 500 and $700 \mathrm{cal} \mathrm{mol}^{-1}$, these results are consistent with all terms in the potential having the same temperature dependence.

The small value of $\xi^{\prime}$ suggests that using only the second term of equation (10) or (11) would provide an excellent fit to the experimental results. It is precisely this term that provides the best one parameter fit to a collection of 46 solutes in the 55 per cent 1132/EBBA mixture [23].

### 5.6. Global fit

In $\S 5.5$, we have seen that the ratio $\xi$ is independent of temperature for $E_{t g}$ values close to $900 \mathrm{cal} \mathrm{mol}^{-1}$, and $\xi^{\prime}$ is independent of temperature for $E_{t g}$ values of 500 to $900 \mathrm{cal} \mathrm{mol}^{-1}$. Constant values of $\xi$ and $\xi^{\prime}$ are consistent with the reasonable guess that all contributions to the short range anisotropic potential have similar temperature dependence. In such a case, it is possible to calculate the parameters $\xi$ and $\xi^{\prime}$ in a single least squares fit to all the experimental quadrupolar splittings at all temperatures for a given liquid crystal mixture. In addition, it is possible to determine the $E_{t g}$ value in the same fit, since $E_{t g}$ is independent of temperature. To reduce the number of adjustable parameters in such a fit, it is useful to choose some functional form for the temperature dependence of $k_{z}$ and $k_{\mathrm{s}}$. The variations of $k_{\mathrm{z}}$ and $k_{\mathrm{s}}$ from the individual fits to each temperature above resemble parabolas. To an excellent approximation, these $k_{z}$ and $k_{\mathrm{s}}$ can be approximated by

$$
\begin{equation*}
k_{i}=k_{0}+k_{1} *\left(1-T_{\mathrm{r}}\right)+k_{2} *\left(1-T_{\mathrm{r}}\right)^{1 / 2} . \tag{12}
\end{equation*}
$$

Using this functional form in a fit to all experiments for a given sample at all temperatures gives the fitted parameters $k_{0}, k_{1}$ and $k_{2}, \xi$ (or $\xi^{\prime}$ ), $E_{t g}$ and $\theta$ in table 5 for the CZ model and in table 6 for the CI model.

### 5.6.1. Global fit model parameters

It is instructive to compare the fitted parameters $k_{z}\left(k_{\mathrm{s}}\right), \xi\left(\xi^{\prime}\right)$ and $E_{t g}$ to those from previous studies. First, we compare the parameters $\left(k_{z}, \xi\right)$ and $\left(k_{\mathrm{s}}, \xi^{\prime}\right)$ to the values obtained from a study of 46 solutes in 55 per cent 1132/EBBA at 301 K [23]. The $k_{z}$ value for the 55 per cent $1132 / E B B A$ at 301 K in our study is $3.13 \mathrm{dyn} \mathrm{cm}^{-1}$, which is close to the value $4.00 \mathrm{dyn} \mathrm{cm}^{-1}$ found in the study of 46 solutes in 55 per cent $1132 / \mathrm{EBBA}$ at 301 K [23]. However, the ratio $\xi$ is -2.20 in our study and -3.9 for the 46 solutes [23]. Although the $k_{z}$ values in these two studies are close, the ratio $\xi$ in our study is much smaller than that for the 46 solutes [23]. Similarly, the fitted $k$ and $k_{\mathrm{s}}$ values are 2.22 and 6.08 in our study compared to 2.04 and 48.0 for the 46 solutes in 55 per cent $1132 / E B B A$ at 301 K [23].

Next, we compare the fitted $E_{t g}$ values to those in the literature. The fitted $E_{t g}$ values for 55 per cent $1132 /$ EBBA are 952 and $1001 \mathrm{cal} \mathrm{mol}^{-1}$ and those for 70 per cent 5CB/EBBA are 911 and $972 \mathrm{cal} \mathrm{mol}^{-1}$ using the CZ (see table 5) and CI (see table 6) models. These $E_{t g}$ values are high compared to most accepted literature values [24,33-36] which are close to $500 \mathrm{cal} \mathrm{mol}^{-1}$. However, we note that one study reports the value $966 \mathrm{cal} \mathrm{mol}^{-1}$ for $E_{t g}$ of gaseous $n$-butane [32].

Since the fitted $E_{t g}$ values are high compared to commonly accepted literature values ( $400-700 \mathrm{cal} \mathrm{mol}^{-1}$ ), we shall explore the possibility of using a more acceptable value. For this purpose, we consider the RMS plots given in figure 5. For the CI model, the

Table 5. Fitted parameters of the CZ model using the PERP-0 geometry and varying $E_{t g}$. For a given liquid crystal mixture, the fit is to all experimental quadrupolar splittings at all temperatures. The $k_{i}$ describe the temperature dependence of the model parameter $k_{z}$ according to equation (12).

| Fitted parameters | 55 per cent $1132 / \mathrm{EBBA}$ | 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ |
| :---: | :---: | :---: |
| $k_{0} / \mathrm{dyne}_{\mathrm{cm}}{ }^{-1}$ | $0.94 \pm 0.06$ | $1.11 \pm 0.03$ |
| $k_{1} / \mathrm{dyne}^{-1}$ | $-2.28 \pm 1.04$ | $-1.05 \pm 1.07$ |
| $k_{2} / \mathrm{dynem}^{-1}$ | $7.47 \pm 0.50$ | $5.41 \pm 0.38$ |
| $\xi$ | $-2.20 \pm 0.23$ | $-2.73 \pm 0.32$ |
| $E_{t g} / \mathrm{cal} \mathrm{mol}^{-1}$ | $952 \pm 19$ | $911 \pm 21$ |
| $\theta / \mathrm{deg}^{2}$ | $118.94 \pm 0.03$ | $118.74 \pm 0.03$ |
| $\mathrm{RMS} / \mathrm{Hz}$ | 1089 | 968 |

Table 6. Fitted parameters of the CI model using the PERP-4 geometry and varying $E_{t g}$. For a given liquid crystal mixture, the fit is to all experimental quadrupolar splittings at all temperatures. The $k_{i}$ describe the temperature dependence of the model parameter $k_{\mathrm{s}}$ according to equation (12).

| Fitted parameters | 55 per cent $1132 / \mathrm{EBBA}$ | 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ |
| :---: | :---: | :---: |
| $k_{0} /{\text { dyne } \mathrm{cm}^{-1}} /$ | $-5.34 \pm 1.48$ | $-5.57 \pm 2.00$ |
| $k_{1} / \mathrm{dynnem}^{-1}$ | $30.68 \pm 8.27$ | $18.63 \pm 6.73$ |
| $k_{2} / \mathrm{dynecm}^{-1}$ | $-35.13 \pm 9.39$ | $-21.84 \pm 7.71$ |
| $\xi^{\prime}$ | $-0.16 \pm 0.05$ | $-0.19 \pm 0.08$ |
| $E_{t g} / \mathrm{cal} \mathrm{mol}^{-1}$ | $1001 \pm 23$ | $972 \pm 23$ |
| $\theta / \mathrm{deg}$ | $119.68 \pm 0.05$ | $119.58 \pm 0.08$ |
| RMS/Hz | 946 | 1006 |

$E_{t g}$ value $700 \mathrm{cal} \mathrm{mol}^{-1}$ gives acceptable fits, although larger $E_{t g}$ values give better fits. Moreover, $\xi^{\prime}$ is independent of temperature when $E_{t g}$ takes the value $700 \mathrm{cal} \mathrm{mol}^{-1}$. For the CZ model, the ratio $\xi$ is independent of temperature for high $E_{t g}$ values. However, the $E_{\mathrm{tg}}$ value $700 \mathrm{cal} \mathrm{mol}^{-1}$ gives acceptable fits, and the ratio $\xi$ is less dependent on temperature than for $E_{t g}$ of $500 \mathrm{calmol}^{-1}$. As a result, we chose the $E_{t g}$ value $700 \mathrm{cal} \mathrm{mol}^{-1}$, which is also the upper limit of the acceptable $E_{t g}$ range, and repeated the least squares minimization keeping the $E_{t g}$ value fixed at $700 \mathrm{cal} \mathrm{mol}^{-1}$ and adjusting the parameters $k_{0}, k_{1}, k_{2}, \theta$, and $\xi$ or $\xi^{\prime}$.

The fitted values of $k_{0}, k_{1}, k_{2}, \theta$, and $\xi$ or $\xi^{\prime}$ are reported in table 7 or table 8 for the $E_{t g}$ value $700 \mathrm{cal} \mathrm{mol}^{-1}$. The RMS deviation in these fits is larger than when $E_{t g}$ was varied, but the fits are still quite acceptable. We again compare the fitted values with those from the study of 46 solutes in 55 per cent $1132 / \mathrm{EBBA}$. The $k_{z}$ and $\xi$ values are 4.03 and -4.02 in our study, whereas these values are 3.92 and -5.01 in the study of 46 solutes [23]. This is excellent agreement. In addition, the fitted $k$ and $k_{\mathrm{s}}$ values in our study are -0.80 and 76.4 compared to 2.04 and 48.0 in [23]. However, the $k_{\mathrm{s}}$ value $76.4 \mathrm{dyn} \mathrm{cm}^{-1}$ is very close to the $k_{\mathrm{s}}$ value $76.7 \mathrm{dyn} \mathrm{cm}^{-1}$ [23] obtained for the 46 solutes when the short range potential, $U_{\mathrm{st}, i}(\Omega)$, is expressed only in terms of $k_{\mathrm{s}}$ (i.e. $k=0$ ). This is consistent with the separate fits at each temperature of $k$ and $k_{\mathrm{s}}, \S 5.5$, where it was found that the $k_{\mathrm{s}}$ term dominates the potential.

Table 7. Fitted parameters of the CZ model using the PERP-0 geometry and fixing $E_{t g}$ at $700 \mathrm{cal} \mathrm{mol}^{-1}$. For a given liquid crystal mixture, the fit is to all experimental quadrupolar splittings at all temperatures. The $k_{i}$ describe the temperature dependence of the model parameter $k_{z}$ according to equation (12).

| Fitted parameters | 55 per cent $1132 / \mathrm{EBBA}$ | 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ |
| :---: | :---: | :---: |
| $k_{0} /$ dyne cm $^{-1}$ | $0.83 \pm 0.12$ | $1.08 \pm 0.05$ |
| $k_{1} / \mathrm{dyne} \mathrm{cm}^{-1}$ | $1.66 \pm 1.96$ | $2.29 \pm 1.30$ |
| $k_{2} / \mathrm{dyne}^{-1}$ | $9.25 \pm 1.07$ | $6.39 \pm 0.59$ |
| $\xi$ | $-4.02 \pm 0.11$ | $-4.79 \pm 0.14$ |
| $E_{t g} / \mathrm{cal}^{-1} \mathrm{~mol}^{-1}$ | 700.00 | 700.00 |
| $\theta / \mathrm{deg}^{\text {RMS } / \mathrm{Hz}}$ | $119.38 \pm 0.04$ | $119.27 \pm 0.04$ |
|  | 1594 | 1405 |

Table 8. Fitted parameters of the CI model using the PERP-4 geometry and fixing $E_{t g}$ at $700 \mathrm{cal} \mathrm{mol}^{-1}$. For a given liquid crystal mixture, the fit is to all experimental quadrupolar splittings at all temperatures. The $k_{i}$ describe the temperature dependence of the model parameter $k_{\mathrm{s}}$ according to equation (12).

| Fitted parameters | 55 per cent $1132 / \mathrm{EBBA}$ | 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ |
| :---: | :---: | :---: |
| $k_{0} / \mathrm{dyne} \mathrm{cm}^{-1}$ | $-25.27 \pm 1.49$ | $-28.55 \pm 1.28$ |
| $k_{1} / \mathrm{dyne} \mathrm{cm}^{-1}$ | $115.05 \pm 16.67$ | $78.05 \pm 15.46$ |
| $k_{2} /$ dyne $\mathrm{cm}^{-1}$ | $-147.87 \pm 10.39$ | $-102.59 \pm 8.15$ |
| $\xi^{\prime}$ | $-0.013 \pm 0.002$ | $-0.013 \pm 0.002$ |
| $E_{t g} / \mathrm{cal} \mathrm{mol}^{-1}$ | 700.00 | 700.00 |
| $\theta / \mathrm{deg}^{\text {RMS } / \mathrm{Hz}}$ | $120.50 \pm 0.04$ | $120.74 \pm 0.06$ |
|  | 1390 | 1464 |

### 5.7. Comparison of short range interactions

In equation (3) we note that all potential terms are divided by $T$. A simple Maier-Saupe mean field theory of nematics [38] would predict a unique value for $U_{\mathrm{sr} i}(\Omega) / T$ at the nematic-isotropic phase transition temperature, $T_{\mathrm{NI}}$. As $T_{\mathrm{NI}}$ varies for different liquid crystals, and as $U_{\mathrm{int}, i}$ is a constant for a given conformer, the $U_{\mathrm{int}, i} / T_{\mathrm{NI}}$ part of the potential for the solute 5 CB at the nematic-isotropic transition will vary inversely with $T_{\mathrm{N} 1}$. The simple Maier-Saupe potential predicts the same reduced temperature, $T_{\mathrm{r}}=T / T_{\mathrm{NI}}$, dependence of the order parameter. Thus differences at $T_{\mathrm{NI}}$ are expected to propagate throughout the nematic temperature range. Could this variation with $T_{\mathrm{Nl}}$ of the $U_{\mathrm{int}, i} / T$ part of the potential account for the observed spectral differences? To examine this possibility in terms of the intra- and inter-molecular potentials acting on 5CB as solute in the nematic mixtures that we are investigating here, we need to analyse the results in terms of the parameters on which these potentials, and thus the quadrupolar splittings, depend.

In $\S 5.5$ we saw that fits to the spectrum obtained at each individual temperature using the $E_{t g}$ value $700 \mathrm{cal} \mathrm{mol}^{-1}$ give very good agreement between the experimental and calculated quadrupolar splittings. In $\S 5.6$ we found that the global fit calculation using the $E_{t g}$ value $700 \mathrm{cal} \mathrm{mol}^{-1}$ gives very good agreement between the fitted model parameters in our study and the parameters found in a study of 46 solutes in the 55 per cent $1132 / E B B A$ zero electric field gradient nematic mixture [13,23]. Therefore, an appropriate choice of $E_{t g}$ for comparison of the short range potentials in the zero electric field gradient mixtures is $700 \mathrm{cal} \mathrm{mol}^{-1}$. The model parameters $k_{i}$ are $k_{z}$ and $k_{x y}$ for the

CZ model, (equation (8)), and $k$ and $k_{\mathrm{s}}$ for the CI model, (equation (10)). Therefore, the quadrupolar splitting of deuteron $j, \Delta v_{j}$, can be written

$$
\begin{equation*}
\Delta v_{j}=f\left(j, \frac{k_{z}}{T}, \frac{k_{x y}}{T}, \frac{E_{t g}}{T}\right) \tag{13}
\end{equation*}
$$

for the CZ model with a similar equation for the CI model.
To compare the potentials in the various liquid crystals, it is instructive to plot the calculated $k_{i} / T$ values versus $\Delta v_{1}$. The choice of $\Delta \nu_{1}$ as a plotting parameter requires some explanation. In the quadrupolar splitting versus temperature plot in figure 3 and the $k_{i} / T$ versus reduced temperature plots in figure 6 an unusual temperature dependence was observed for the 70 per cent 5CB/EBBA mixture. Therefore we wish to choose a quantity, other than reduced temperature, for comparison. The first quantity that comes to mind is the order parameter for the sample. However, this quantity is difficult to define, especially for the liquid crystal mixtures used in this work. In addition, a Maier-Saupe mean field theory for binary mixtures of axially symmetric nematic liquid crystals gives the anisotropic part of the mean-field intermolecular potential for particle $i$ as [39-41]

$$
\begin{equation*}
U_{i}(\Omega)=\left[\rho_{i} U_{i i} S_{i}+\rho_{j} U_{i j} S_{j}\right] P_{2}(\cos \Omega) \tag{14}
\end{equation*}
$$

where $\rho_{i}$ is the number density of component $i, U_{i j}$ is the anisotropic interaction strength between components $i$ and $j$, and $S_{i}$ is the order parameter of component $i$. Note that it is easy to extend equation (14) to multicomponent mixtures by adding a $U_{i j}$ term for each component. This potential predicts, in general, different values for the order parameters of components $i$ and $j$. In addition the value of $U_{i}(\Omega) / T$ for a given liquid crystal $i$ will not necessarily be the same at a given reduced temperature in different mixtures; this could explain some of the difference between mixtures observed in figure 6. As we wish to compare the intermolecular potential acting on our solute 5 CB in the different liquid crystal mixtures, it would make sense to choose for comparison situations where the order parameter of the solute is the same. In terms of equation (14) for an axially symmetric nematic, this would require that $U_{i}(\Omega) / T$ be the same in both mixtures. In the real case, 5CB is not axially symmetric, and exists in many conformations. Thus the test for similar potentials would be that the various contributions to the potential, i.e. the two terms in equations (8) to (11) or the terms in equation (14), divided by temperature, give equal contributions to the total potential. Fortunately the lack of symmetry in 5CB allows us to fit our spectral results to potentials with more than one parameter: the comparison between mixtures than involves comparison of these parameters.

As an aside, equation (14) has also been used to describe mixtures of a nematic liquid crystal with a solute that does not itself exhibit a liquid crystalline phase [42]. Thus, for all solutes $i$ to experience the same anisotropic potential in different liquid crystal mixtures, in terms of equation (14) it is required that $U_{i k}=c_{k j} \times U_{i j}$ with $c_{k j}$ a constant depending only on liquid crystal components $j$ and $k$, but being independent of solute $i$. Note that the requirement for a zero field gradient mixture is that for all solutes the anisotropic components of the field gradient cancel when terms for all component liquid crystals are added.

Because of the lack of symmetry and the intramolecular motions in 5CB, the choice of its order parameter for comparison purposes presents a problem. A more convenient choice would be the quadrupolar splittings $\Delta v_{j}$ of $5 \mathrm{CB}-d_{19}$ which are related to this order parameter. But which splitting is the best to use? Note that we are interested in
separating the temperature effects of the $U_{\mathrm{int}, i}$ and $U_{\mathrm{sr} i}(\Omega)$. In a calculation of the quadrupolar splittings of $5 \mathrm{CB}-d_{19}$ at two different temperatures having the same $k_{i} / T$ values, we found that the quadrupolar splitting $\Delta v_{1}$ is the least dependent upon the $E_{t g} / T$ term. Thus it is appropriate to use $\Delta v_{1}$ for comparing the liquid crystal mixtures.

To examine the liquid crystal mixture dependence of the $k_{i}$ parameters, we plot $k_{z} / T$, $k_{x y} / T, k_{\mathrm{s}} / T$ and $k / T$ versus $\Delta v_{1}$ in figures $8-11$. The $k_{i}$ values in these plots are those that were obtained from a separate least squares fitting for each spectrum at each different temperature. The plots in these figures show that for a given $\Delta v_{1}$, the $k_{i} / T$ values of 55 per cent 1132/EBBA are in excellent agreement with those of 70 per cent 5CB/EBBA. Based on this agreement, we can write for a given $\Delta v_{1}$

$$
\begin{equation*}
\left(k_{i} / T\right)_{55}=\left(k_{i} / T\right)_{70} \tag{15}
\end{equation*}
$$

where $k_{i} / T$ can be $k_{z} / T, k_{x y} / T, k_{s} / T$ or $k / T$. The subscripts 55 and 70 stand for the liquid crystal mixtures 55 per cent 1132/EBBA and 70 per cent 5CB/EBBA. This demonstrates that the choice of $\Delta \nu_{1}$ (as a parameter proportional to the 5 CB order parameter) for comparison purposes was a good one. Because the two parameters describing the potential scale in the same way, figures 8 to 11 demonstrate that the anisotropic short range potentials in 55 per cent $1132 / \mathrm{EBBA}$ and 70 per cent $5 \mathrm{CB} / E B B A$ are the same. Substituting equation (15) into equations (8) and (10), we obtain for a given $\Delta v_{1}$

$$
\begin{equation*}
\left(U_{\mathrm{sr}} / T\right)_{55}=\left(U_{\mathrm{sr}} / T\right)_{70} \tag{16}
\end{equation*}
$$

Thus, for a given $\Delta v_{1}$, the experimental results are described by the same reduced short range potentials and reduced model parameters for both zero electric field gradient mixtures. This conclusion is independent of the model chosen for analysis. Note that by a reduced quantity we mean the actual quantity divided by temperature.

As the purpose of this paper is to examine several zero electric field gradient mixtures and to investigate to what extent the description of the anisotropic short range potential is similar in the various mixtures, it is worthwhile analysing equations (15) and (16) further. As pointed out above, one way of emphasizing small differences among zero electric field gradient mixtures is to plot ratios of the quadrupolar splittings, such as $\Delta v_{5} / \Delta v_{1}$, against $\Delta v_{1}$. In figure 4 we chose the ratio $\Delta v_{5} / \Delta v_{1}$ for comparison, because the quadrupolar splittings at the 5 -position are more difficult to fit than the quadrupolar splittings at other positions of the chain. This is because the methyl deuterons are sensitive to all internal chain motions. However, qualitatively similar results are obtained for other chain positions.

In figures 12 and 13 we compare experimental ratios from figure 4 (filled symbols) with those recalculated from the best-fit parameters obtained from separate fits to each experimental spectrum in $\S 5.5$ (dotted symbols). Figure 12 presents results for the CZ model, and figure 13 for the CI model. Although there is a deviation between the calculated and experimental quadrupolar splitting ratios, the general experimental trends are observed with both models. More important, the differences between the liquid crystal mixtures are well predicted. The deviation between experiment and theory is mainly due to the inadequacy of the models.

We now turn to the question 'If the intermolecular potential is the same, why do the quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ differ with liquid crystal solvent in the ratio plots of figures 12 and 13?' Equation (13) tells us that there is another parameter, $E_{t g} / T$, on which the quadrupolar splitting $\Delta v_{j}$ depends. The value of $E_{t g}$ is constant, and is set to $700 \mathrm{cal} \mathrm{mol}^{-1}$. However, the temperature at which a given $\Delta v_{1}$ is observed in the 55


Figure 8. Reduced model parameter, $k_{z} / T(C Z$ model, PERP-0 geometry), against quadrupolar splitting $\Delta v_{1}$ for the $E_{t g}$ value $700 \mathrm{cal} \mathrm{mol}{ }^{-1}$. Open squares ( $\square$ ) 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$. Closed squares ( 1 ) 55 per cent $1132 / \mathrm{EBBA}$.


Figure 9. Reduced model parameter, $k_{x y} / T$ (CZ model, PERP-0 geometry), against quadrupolar splitting $\Delta v_{1}$ for the $E_{t g}$ value $700 \mathrm{cal} \mathrm{mol}^{-1}$. Open squares ( $\square$ ) 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$. Closed squares ( $\square$ ) 55 per cent $1132 / \mathrm{EBBA}$.


Figure 10．Reduced model parameter，$k_{\mathrm{s}} / T$（CI model，PERP－4 geometry），against quadrupolar splitting $\Delta v_{1}$ for the $E_{f g}$ value $700 \mathrm{cal} \mathrm{mol}^{-1}$ ．Open squares（ $\square$ ） 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ ．Closed squares（⿴囗十⿱一⿴⿻儿口一寸 ） 55 per cent $1132 / \mathrm{EBBA}$ ．


Figure 11．Reduced model parameter，$k / T$（CI model，PERP－4 geometry），against quadrupolar splitting $\Delta v_{1}$ for the $E_{t g}$ value $700 \mathrm{cal} \mathrm{mol}{ }^{-1}$ ．Open squares（ $\square$ ） 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ ． Closed squares（■） 55 per cent $1132 / E B B A$ ．


Figure 12. Quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ versus $\Delta v_{1}$ (CZ model, PERP-0 geometry). Individual fit $C Z$ model parameters were used to calculate the recalculated (dotted symbols and line) and 'scaled' (solid line) quadrupolar splitting ratios.


Figure 13. Quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ versus $\Delta v_{1}$ (CI model, PERP-4 geometry). Individual fit CI model parameters were used to calculate the recalculated (dotted symbols and line) and 'scaled' (solid line) quadrupolar splitting ratios.

Table 9. Temperature scaling factors, TSF (see text).

| $T_{70} / \mathrm{K}$ of 70 per cent 5CB/EBBA | TSF | $T_{70} / \mathrm{K}$ of 70 per cent 5CB/EBBA | TSF |
| :---: | :---: | :---: | :---: |
| 251.9 | 1.114 | 296.6 | 1.077 |
| 255.9 | 1.117 | 302.0 | 1.069 |
| 261.2 | 1.107 | 306.8 | 1.061 |
| 265.3 | 1.108 | 308.8 | 1.058 |
| 271.1 | 1.106 | 310.8 | 1.058 |
| 276.1 | 1.097 | 312.7 | 1.062 |
| 281.9 | 1.094 | 313.7 | 1.061 |
| 285.9 | 1.092 | 314.7 | 1.065 |
| 292.1 | 1.082 | 315.7 | 1.065 |
|  |  | TSF $_{\text {average }}$ | 1.083 |

per cent 1132/EBBA mixture, $T_{55}$, is different from that in the 70 per cent 5CB/EBBA mixture, $T_{70}$. As a result, the $E_{t g} / T$ term is different for the two mixtures. Therefore, the differences in quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ must be due to the different temperatures ( $T_{55}$ and $T_{70}$ ) associated with the different liquid crystal mixtures 55 per cent $1132 / \mathrm{EBBA}$ and 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$.

Of course, the above analysis is based on independent fits of spectra in the different mixtures. Perhaps a better demonstration that the spectral differences are due to the temperature dependence of the conformational averaging would be to predict the spectrum of one mixture from the $k_{i}$ parameters of the other mixture. We shall call the quadrupolar splittings of these predicted spectra 'scaled quadrupolar splittings'.

In this study, we shall start from the reduced model parameters of 70 per cent 5CB/EBBA and shall predict the quadrupolar splittings of the 55 per cent 1132/EBBA mixture. In order to predict the quadrupolar splittings in 55 per cent 1132/EBBA, it is necessary to use the appropriate temperatures in the $E_{t g} / T$ term; the temperature in the $E_{t g} / T$ term has to be scaled by a factor $T_{55} / T_{70}$. In order to simplify the notation, we define this factor $T_{55} / T_{70}$ as the temperature scaling factor (TSF). The TSF values are calculated from the results for a given $\Delta v_{1}$ and tabulated with the corresponding temperatures of the 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ mixture in table 9 . For each entry in table 9 , the reduced short range potentials $U_{\mathrm{sr}, i}(\Omega) / T$ along with $U_{\mathrm{int}, i} /\left(T_{70} \times\right.$ TSF $)$ are used to calculate the 'scaled quadrupolar splittings'. If we are correct that the spectral differences arise from the temperature effect on the conformational averaging, these scaled splittings should equal the recalculated splittings of $5 \mathrm{CB}-d_{19}$ in the 55 per cent $1132 / \mathrm{EBBA}$ mixture. To demonstrate that this is indeed the case, we plot 'scaled' along with experimental and recalculated quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ in figure 12 ( CZ model) and 13 (CI model). The agreement between the 'scaled' (thick lines, predicted from the results of the 70 per cent 5 CB/EBBA experiments) and recalculated (dotted lines, fits to the 55 per cent $1132 / E B B A$ experiments themselves) quadrupolar splitting ratios is excellent for the $C Z$ model. This agreement confirms that the differences in the quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ come from the different temperatures $T_{55}$ and $T_{70}$ of 55 per cent $1132 /$ EBBA and 70 per cent 5 CB/EBBA for a given $\Delta v_{1}$. For a given value of $U_{\mathrm{ss}, i}(\Omega) / T$, the different temperatures affect the quadrupolar splittings via the effect of the different $U_{\mathrm{int}, i} / T$ on the conformational averaging.

In $\S 5.6$ the results were analysed by fitting all spectra at all temperatures in a given liquid crystal solvent to a set of global parameters. In these fits the ratio between the $k_{i}$ values, $\xi$ or $\xi^{\prime}$, were kept constant for a given solvent. Above we have seen that, for


Figure 14. Quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ versus $\Delta v_{1}$ (CZ model, PERP-0 geometry). Global fit CZ model parameters were used to calculate the recalculated (dotted symbols and line) and 'scaled' (solid line) quadrupolar splitting ratios.


Figure 15. Quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ versus $\Delta v_{1}$ (CI model, PERP-4 geometry). Global fit CI model parameters were used to calculate the recalculated (dotted symbols and line) and 'scaled' (solid line) quadrupolar splitting ratios.
a given experimental $\Delta v_{1}$, the reduced model parameters are transferable from one zero electric field gradient mixture to another and the reduced short range potentials of the two zero electric field gradient mixtures are equal. The global fit parameters can be tested in a similar analysis.

First, we shall examine the fitted parameters in tables 7 and 8 corresponding to $E_{t g}$ of $700 \mathrm{cal} \mathrm{mol}^{-1}$. Based on equation (15), we intuitively expect that the ratios $\xi=k_{x y} / k_{z}$ or $\xi^{\prime}=k / k_{\mathrm{s}}$ should be the same in all zero electric field gradient mixtures. The $\xi$ values are -4.02 and -4.79 and the $\xi^{\prime}$ values are -0.013 and -0.013 for the liquid crystal mixtures 55 per cent $1132 /$ EBBA and 70 per cent 5CB/EBBA. The $\xi$ and $\xi^{\prime}$ values of these two liquid crystal mixtures are in excellent agreement. Thus, the ratios $\xi$ and $\xi^{\prime}$ are transferable from one zero electric field gradient mixture to another.

As was the situation above, a most useful comparison is to check the transferability of reduced model parameters by calculating the 'scaled quadrupolar splittings'. We start with the reduced model parameters $k_{0} / T_{70}, k_{1} / T_{70}$ and $k_{2} / T_{70}$ of 70 per cent 5CB/EBBA. Then we use $T=T_{70} \times \mathrm{TSF}_{\text {average }}$ (see table 9 ) in the calculation of $U_{\text {int }, i} / T$ to calculate the 'scaled quadrupolar splittings'.

The 'scaled', experimental and recalculated quadrupolar splitting ratios $\Delta v_{5} / \Delta v_{1}$ are plotted against $\Delta v_{1}$ in figure 14 (CZ model) and 15 (CI model. The agreement between the 'scaled' (solid line, predicted from the results of the 70 per cent 5 CB/EBBA experiments) and recalculated (dotted line, fits to the 55 per cent $1132 / \mathrm{EBBA}$ experiments themselves) quadrupolar splitting ratios is excellent for the CI model. In addition, the fits are in reasonable agreement with the experimental results, and the general features of the experimental quadrupolar splittings are predicted. In this case a temperature independent $\xi^{\prime}$ seems the correct choice. For the CZ model, however, the fits are not as good. This is because the $\xi$ parameter was kept constant with temperature. Above it was shown for this model with $E_{t g} \leq 700 \mathrm{cal} \mathrm{mol}^{-1}$ that the best results are obtained with a temperature dependent $\xi$. This is evident from the deviation between the experimental and recalculated quadrupolar splitting ratios in figure 14. The 'scaled quadrupolar splitting' ratios agree well with the recalculated quadrupolar splitting ratios at high temperatures. However, the deviation is large for low temperatures. This deviation is partly due to the fact that the TSF ratios, $T_{55} / T_{70}$, at low temperatures are very different from the $\operatorname{TSF}_{\text {average }}(1 \cdot 083)$ whereas these ratios are very close to the TSF average at high temperatures.

## 6. Conclusions

The quadrupolar splittings of $5 \mathrm{CB}-d_{19}$ in the zero efg mixtures 55 per cent 1132/EBBA and 56.5 per cent $1132 / \mathrm{EBBA}$ are almost equal at any given temperature. Therefore, the short range potentials in these two mixtures are the same. However, the quadrupolar splittings of $5 \mathrm{CB}-d_{19}$ in the zero efg mixture 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$ are different from those of 55 per cent $1132 /$ EBBA at any given temperature. These differences at a given temperature are due to the different magnitudes of the short range potentials in these mixtures. The CZ and CI models describing the short range potentials are both successful in calculating the quadrupolar splittings of $5 \mathrm{CB}-d_{19}$ in the mixtures 55 per cent $1132 / \mathrm{EBBA}$ and 70 per cent $5 \mathrm{CB} / \mathrm{EBBA}$. In both cases the trans-gauche energy difference is consistent with the upper range of acceptable values, $700 \mathrm{kcal} \mathrm{mol}^{-1}$. The model parameters $k_{z}$ and $k_{x y}$ of the CZ model and $k$ and $k_{\mathrm{s}}$ of the CI model are useful in comparing the short range potentials between these two mixtures. The values obtained agree quite well with those obtained from a study of 46 solutes in a zero efg nematic solvent.

In this paper we have demonstrated in several different ways that for a given experimental $\Delta v_{1}$ the reduced model parameters $k_{i} / T$ of 55 per cent $1132 /$ EBBA are the same as those of 70 per cent 5 CB/EBBA. That is, irrespective of the model used for analysis, the reduced short range potential appears to be the same in all zero electric field gradient nematic mixtures. In other words, the quadrupolar splittings of 5CB- $d_{19}$ in one zero electric field gradient mixture can be predicted knowing the reduced model parameters of another zero electric field gradient mixture. The differences in spectra between mixtures, and in ratio plots such as those of figure 4 , result from the temperature dependence of the internal energy contribution to the conformer probabilities.

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